

Quantum Molecular Dynamics Simulations

Aiichiro Nakano

*Collaboratory for Advanced Computing & Simulations
Depts. of Computer Science, Physics & Astronomy, Chemical
Engineering & Materials Science, and Biological Sciences
University of Southern California*

Email: anakano@usc.edu

QXMD tutorial:

**Subodh Tiwari, Lindsay Bassman,
Aravind Krishnamoorthy,
Ken-ichi Nomura**



MAGICS Workshop

November 12, 2018, Washington, DC



Additional Resources

Detailed lecture notes are available at a USC course home page

EXTREME-SCALE QUANTUM SIMULATIONS

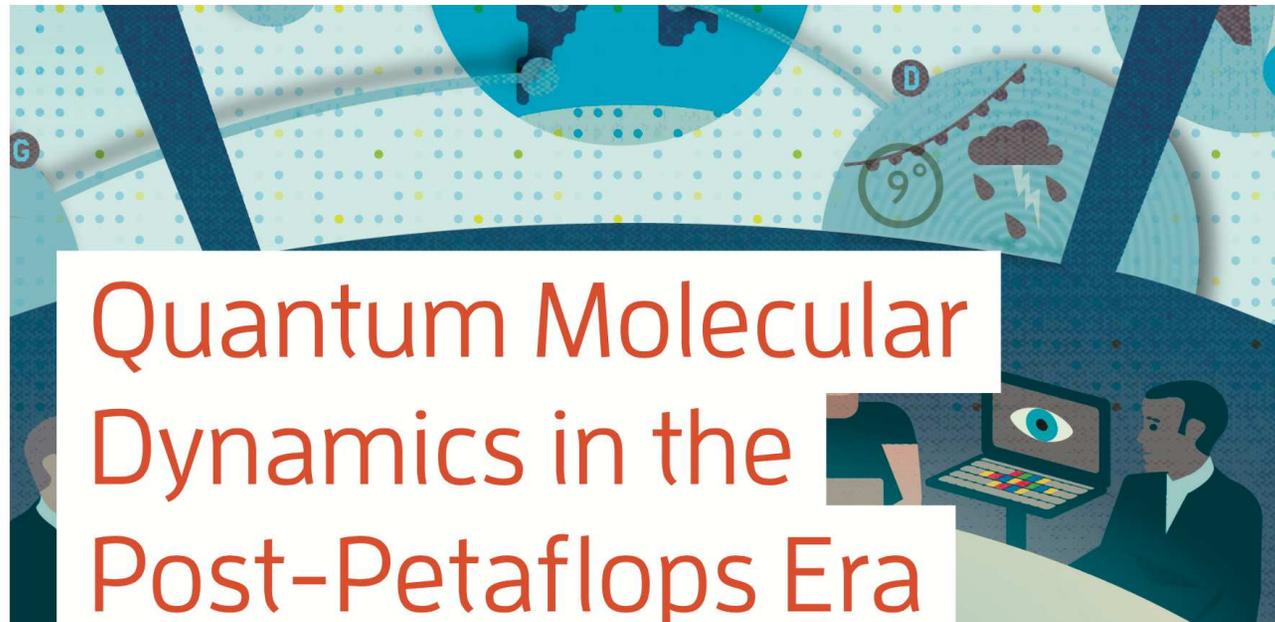
This course surveys & projects algorithmic & computing technologies that will make quantum-dynamics simulations metascalable, *i.e.*, "design once, continue to scale on future computer architectures".

<http://cacs.usc.edu/education/cs699-lecture.html>

See also N. Romero *et al.*, *IEEE Computer* **48(11)**, 33 ('15)

<http://cacs.usc.edu/education/cs653/Romero-QMD-IEEEComputer15.pdf>

COVER FEATURE **GRAND CHALLENGES IN SCIENTIFIC COMPUTING**

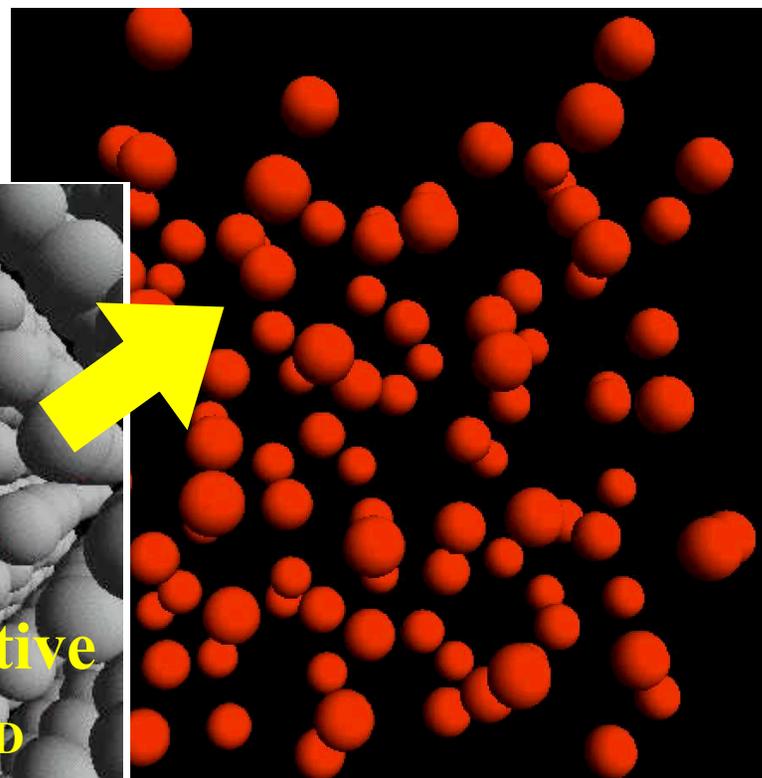
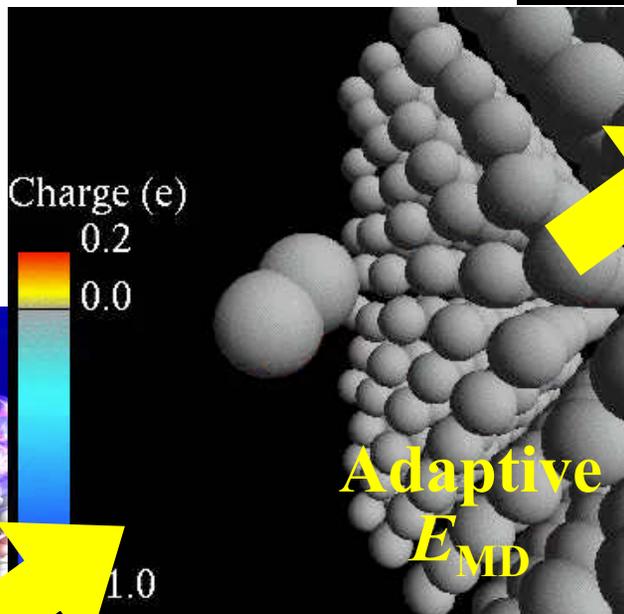
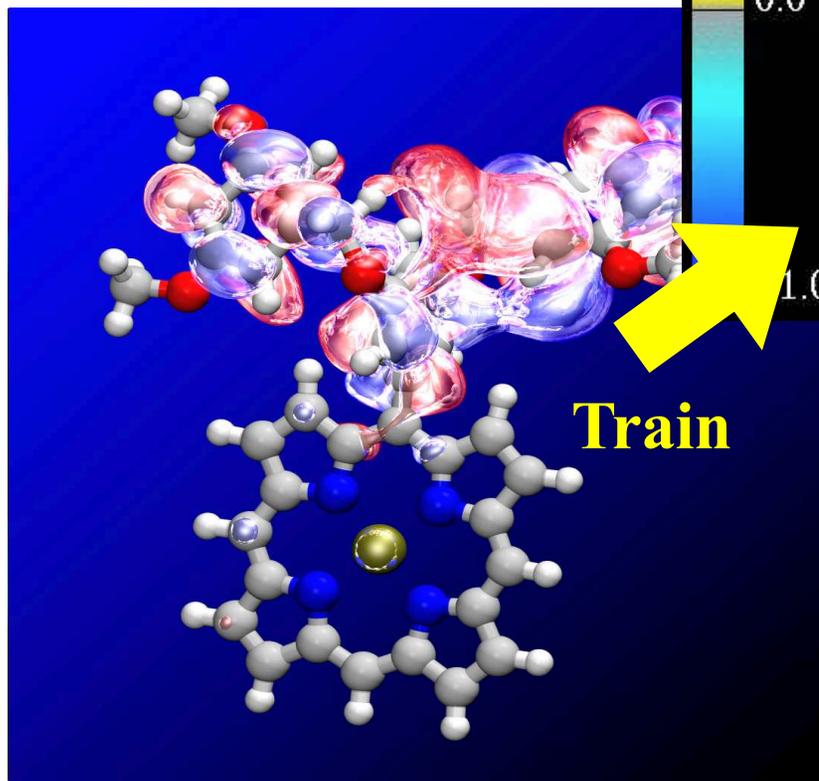


Molecular Dynamics Hierarchy

Molecular Dynamics (MD)

Reactive MD (RMD)

Nonadiabatic quantum MD (NAQMD)



First principles-based reactive force-fields

- Reactive bond order $\{BO_{ij}\}$
→ Bond breakage & formation
- Charge equilibration (QEq) $\{q_i\}$
→ Charge transfer

Quantum Molecular Dynamics (QMD)

$$M_I \frac{d^2}{dt^2} \mathbf{R}_I = - \frac{\partial}{\partial \mathbf{R}_I} E[\{\mathbf{R}_I\}, \psi(\mathbf{r}_1 \dots, \mathbf{r}_N)] \quad (I = 1, \dots, N_{\text{atom}})$$

First molecular dynamics using an empirical interatomic interaction

A. Rahman, *Phys. Rev.* **136**, A405 ('64)



$$\psi(\mathbf{r}_1 \dots, \mathbf{r}_N) \leftarrow \operatorname{argmin} E[\{\mathbf{R}_I\}, \psi(\mathbf{r}_1 \dots, \mathbf{r}_N)]$$

Density functional theory (DFT)

Hohenberg & Kohn, *Phys. Rev.* **136**, B864 ('64)

W. Kohn, *Nobel chemistry prize*, '98

$O(C^N)$ \rightarrow $O(N^3)$
1 N -electron problem \rightarrow N 1-electron problems
intractable **tractable**

$$\psi(\mathbf{r}_1 \dots, \mathbf{r}_N) \quad \{\psi_i(\mathbf{r}) | i = 1, \dots, N\}$$

$O(N)$ DFT algorithms

- **Divide-&-conquer DFT** [W. Yang, *Phys. Rev. Lett.* **66**, 1438 ('91); F. Shimojo *et al.*, *Comput. Phys. Commun.* **167**, 151 ('05); *Phys Rev. B* **77**, 085103 ('08); *Appl. Phys. Lett.* **95**, 043114 ('09); *J. Chem. Phys.* **140**, 18A529 ('14)]
- **Quantum nearsightedness principle** [W. Kohn, *Phys. Rev. Lett.* **76**, 3168 ('96); E. Prodan & W. Kohn, *P. Nat. Acad. Sci.* **102**, 11635 ('05)]
- **A recent review** [Bowler & Miyazaki, *Rep. Prog. Phys.* **75**, 036503 ('12)]

Adiabatic Quantum Molecular Dynamics

- Consider a system of N electrons & N_{atom} nuclei, with the Hamiltonian

$$\begin{aligned}
 \tilde{H} &= \sum_{I=1}^{N_{\text{atom}}} \frac{\mathbf{P}_I^2}{2M_I} + H(\{\mathbf{r}_i\}, \{\mathbf{R}_I\}) \\
 &= \sum_{I=1}^{N_{\text{atom}}} \left[\frac{\mathbf{P}_I^2}{2M_I} + V_{\text{ext}}(\mathbf{R}_I) \right] + \sum_{i=1}^N \left[-\frac{\hbar^2}{2m} \frac{\partial^2}{\partial \mathbf{r}_i^2} + v_{\text{ext}}(\mathbf{r}_i) \right] \\
 &\quad + \frac{1}{2} \sum_{i \neq j} \frac{e^2}{|\mathbf{r}_i - \mathbf{r}_j|} - \sum_{i,J} \frac{Z_J e^2}{|\mathbf{r}_i - \mathbf{R}_J|} + \frac{1}{2} \sum_{I \neq J} \frac{Z_I Z_J e^2}{|\mathbf{R}_I - \mathbf{R}_J|}
 \end{aligned}$$

nucleus momentum
electron position nucleus position
nucleus charge

- In adiabatic quantum molecular dynamics based on Born-Oppenheimer approximation, the electronic wave function remains in its ground state ($|\Psi_0\rangle$) corresponding to the instantaneous nuclei positions ($\{\mathbf{R}_I\}$), with the latter following classical mechanics

$$M_I \frac{d^2}{dt^2} \mathbf{R}_I = -\frac{\partial}{\partial \mathbf{R}_I} \langle \Psi_0 | H(\{\mathbf{r}_i\}, \{\mathbf{R}_I\}) | \Psi_0 \rangle$$

Complexity Reduction: Density Functional Theory

- **P. Hohenberg & W. Kohn, “Inhomogeneous electron gas”**

Phys. Rev. **136**, B864 ('64)

The electronic ground state is a functional of the electron density $\rho(\mathbf{r})$

- **W. Kohn & L. Sham, “Self-consistent equations including exchange & correlation effects”** *Phys. Rev.* **140**, A1133 ('65)

Derived a formally exact self-consistent single-electron equations for a many-electron system



Energy Functional

Exchange-correlation (xc) functional *via* Kohn-Sham decomposition

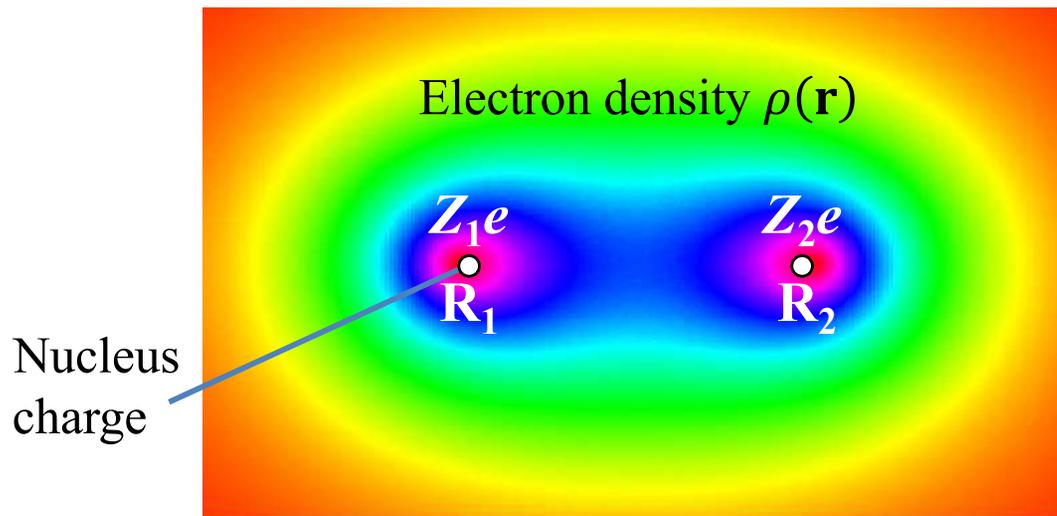
$$E[\rho(\mathbf{r})] = T_s[\rho(\mathbf{r})] + \int d\mathbf{r} v(\mathbf{r})\rho(\mathbf{r}) + \frac{1}{2} \int d\mathbf{r} d\mathbf{r}' \frac{\rho(\mathbf{r})\rho(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} + E_{xc}[\rho(\mathbf{r})]$$

Kinetic energy of
non-interacting
electrons

External potential

Hartree energy (mean-
field approximation to
the electron-electron
interaction energy)

Exchange-correlation
energy



Kohn-Sham Equation

- Many-electron problem is equivalent to solving a set of one-electron Schrödinger equations called Kohn-Sham (KS) equations

$$\left[-\frac{\hbar^2}{2m} \frac{\partial^2}{\partial \mathbf{r}^2} + v_{\text{KS}}(\mathbf{r}) \right] \psi_n(\mathbf{r}) = \epsilon_n \psi_n(\mathbf{r})$$

KS wave function

KS energy

- KS potential

$$v_{\text{KS}} = v(\mathbf{r}) + \int d\mathbf{r}' \frac{e^2 \rho(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} + v_{\text{xc}}(\mathbf{r})$$

exchange-correlation (xc) potential

$$\rho(\mathbf{r}) = \sum_n \Theta(\mu - \epsilon_n) |\psi_n(\mathbf{r})|^2$$

step function chemical potential

$$v_{\text{xc}}(\mathbf{r}) \equiv \frac{\delta E_{\text{xc}}}{\delta \rho(\mathbf{r})}$$

$$N = \sum_n \Theta(\mu - \epsilon_n)$$

W. Kohn & L. J. Sham, "Self-consistent equations including exchange and correlation effects," *Phys. Rev.* **140**, A1133 ('65)

Abstraction: Exchange-Correlation Functional

- **Universal functional (of density) that describes many-body effects beyond the mean-field approximation**
- **Some commonly used exchange-correlation functionals**
 - > **GGA (generalized gradient approximation)**
PBE: Perdew, Burke & Ernzerhof, *Phys. Rev. Lett.* **77**, 3865 ('96)
 - > **MetaGGA**
SCAN: Sun, Ruzsinszky & Perdew, *Phys. Rev. Lett.* **115**, 036402 ('15)
 - > **Hybrid exact-exchange (Hartree-Fock) functionals**
HSE: Heyd, Scuseria & Ernzerhof, *J. Chem. Phys.* **118**, 8207 ('03)
- **Others supported by QXMD code: Select an appropriate functional for the material system & purpose**
 - > **LDA+U method for transition metals**
$$\delta E_{\text{LDA+U}}/\delta n_i = \epsilon_{\text{LDA}} + U\left(\frac{1}{2} - n_i\right)$$

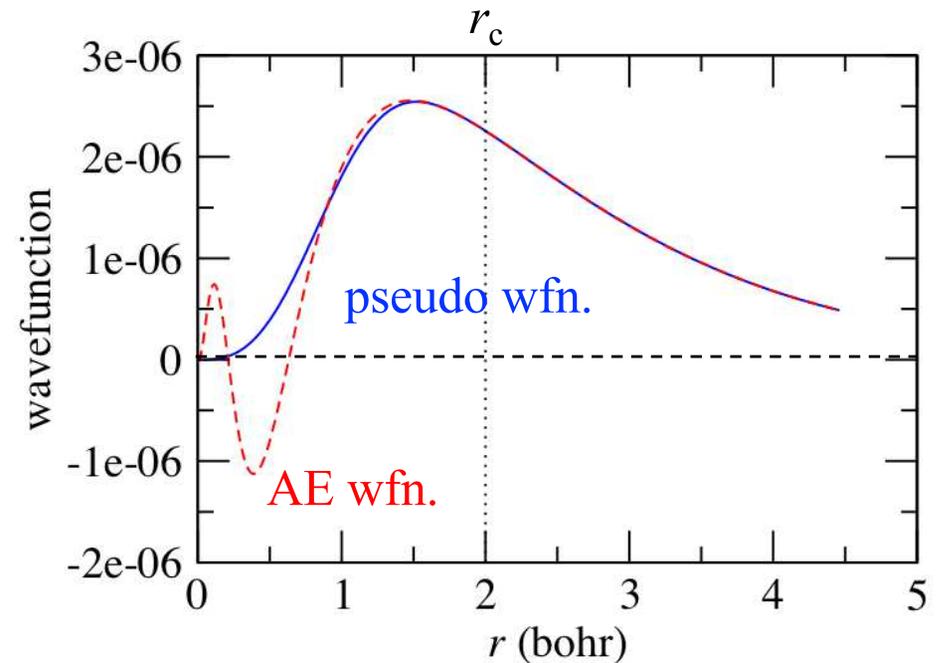
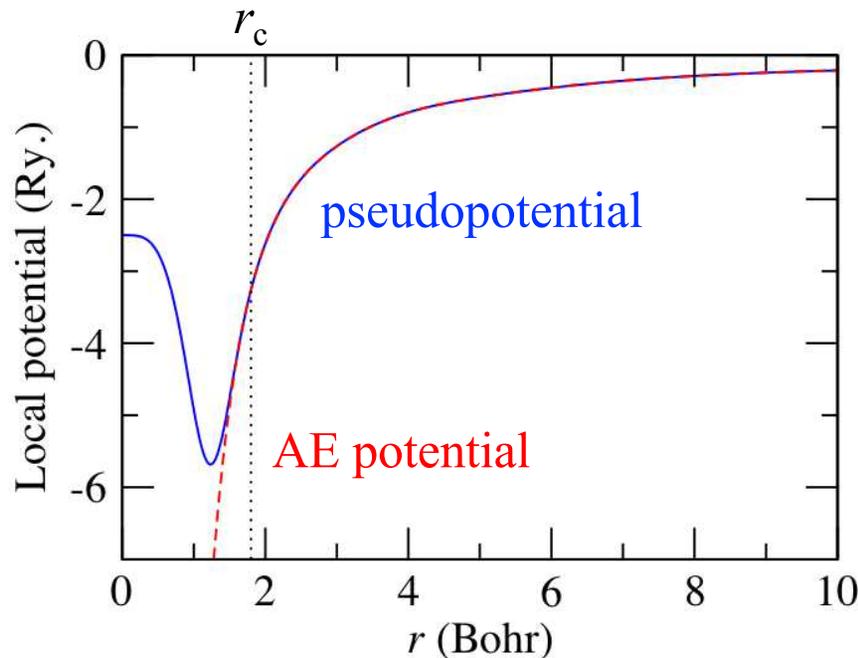
Anisimov *et al.*, *Phys. Rev. B* **44**, 943 ('91)
 - > **DFT-D: van der Waals (vdW) functional for molecular crystals & layered materials**
$$E_{\text{disp}} = -s_6 \sum_{i<j} \frac{c_{ij}}{R_{ij}^6} f_{\text{damp}}(R_{ij})$$

Grimme, *J. Comput. Chem.* **25**, 1463 ('04); *J. Chem. Phys.* **132**, 154104 ('10)
 - > **vdW: Nonlocal correlation functional**
$$E_c^{\text{nl}} = \frac{1}{2} \int d\mathbf{r} \int d\mathbf{r}' \rho(\mathbf{r})\phi(\mathbf{r}, \mathbf{r}')\rho(\mathbf{r}')$$

Dion *et al.*, *Phys. Rev. Lett.* **92**, 246401 ('04)

Abstraction: Pseudopotential

- Consider only (chemically active) valence electrons
e.g. silicon — $1s^2 2s^2 2p^6 3s^2 3p^2$
- Pseudopotentials & smooth, nodeless pseudo-wave functions are constructed to agree with the all-electron (AE) counterparts beyond a cutoff radius r_c



- **Commonly used pseudopotentials**
 - > **Norm-conserving:** Troullier & Martins, *Phys. Rev. B* **41**, 1993 ('91)
 - > **Ultrasoft:** Vanderbilt, *Phys. Rev. B* **41**, 7892 ('90)
 - > **Projector augmented wave (PAW):** Blochl, *Phys. Rev. B* **50**, 17953 ('94)

Self-Consistent Field Iteration

$$\left(-\frac{\hbar^2}{2m} \frac{\partial^2}{\partial \mathbf{r}^2} + \hat{V}_{\text{ion}} + \hat{V}_{\text{H,xc}}[\rho(\mathbf{r})] \right) \psi_n(\mathbf{r}) = \epsilon_n \psi_n(\mathbf{r})$$

Given $\rho(\mathbf{r})$,
iteratively obtain
 $\{\psi_n, \epsilon_n\}$, e.g., by
preconditioned
conjugate gradient

Given $\{\psi_n, \epsilon_n\}$,
determine μ and
compute $\rho(\mathbf{r})$

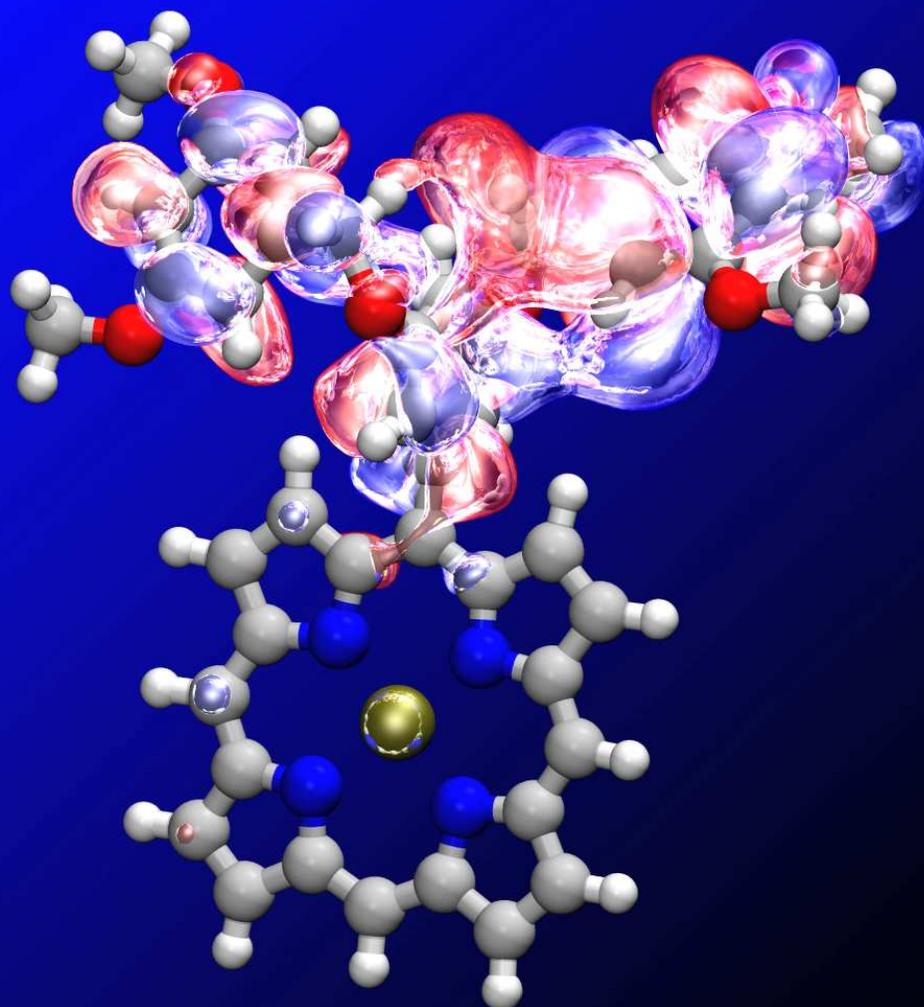
$$\rho(\mathbf{r}) = \sum_n |\psi_n(\mathbf{r})|^2 \Theta(\mu - \epsilon_n)$$

Chemical potential

$$N = \int d\mathbf{r} \rho(\mathbf{r})$$

See **PHYS 516 lecture on iterative energy minimization**
<http://cacs.usc.edu/education/phys516/QD2CG.pdf>

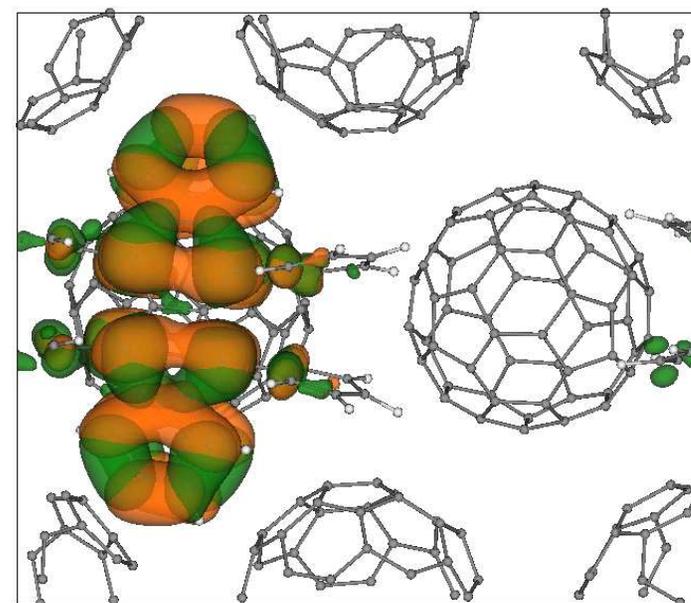
Nonadiabatic Quantum Molecular Dynamics



W. Mou *et al.*, *Appl. Phys. Lett.* **98**, 113301 ('11);
ibid. **100**, 203306 ('12); *J. Chem. Phys.* **136**,
184705 ('12); *Comput. Phys. Commun.* **184**, 1
('13); *Appl. Phys. Lett.* **102**, 093302 ('13); *ibid.*
102, 173301 ('13); *J. Chem. Phys.* **140**, 18A529
('14); *IEEE Computer* **48(11)**, 33 ('15); *Sci. Rep.* **5**,
19599 ('16); *Nature Commun.* **8**, 1745 ('17)

Zn porphyrin

Rubrene/C₆₀



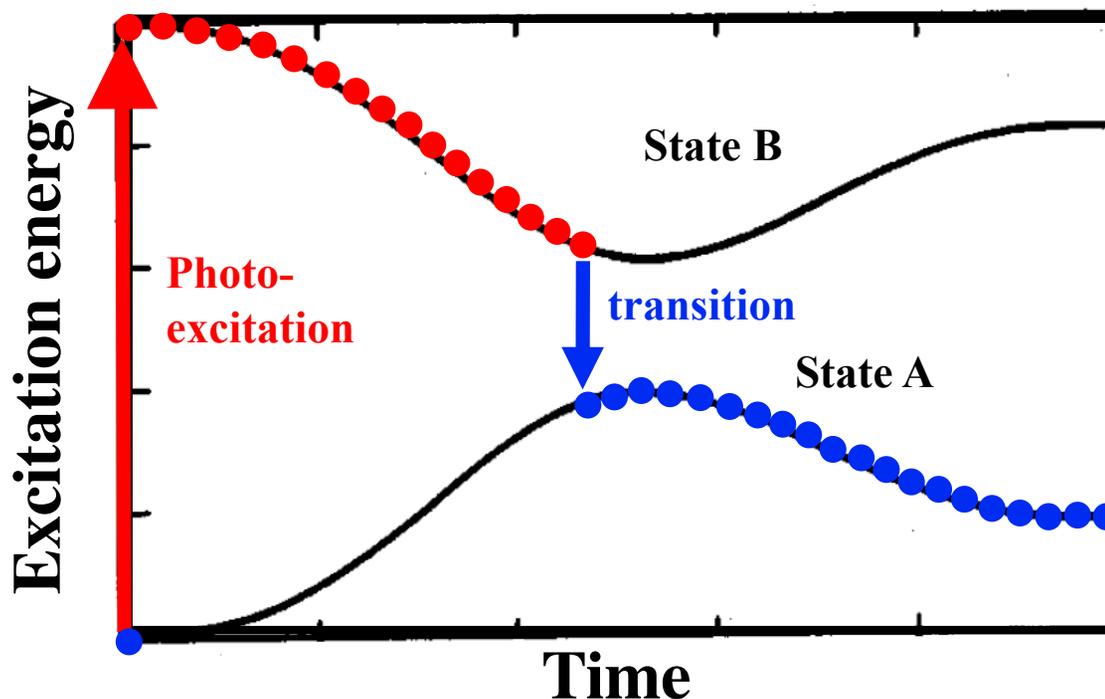
quasi-electron; quasi-hole

- **Excited states:** Linear-response time-dependent density functional theory [Casida, '95]
- **Interstate transitions:** Surface hopping [Tully, '90; Jaeger, Fisher & Prezhdo, '12]

Surface-Hopping NAQMD

- Incorporate electron transitions with the time-dependent density-functional theory (TDDFT) & surface-hopping method

Tully, *J. Chem. Phys.* **93**, 1061 ('90), *ibid.* **129**, 044104 ('08) ; Duncan *et al.*, *J. Am. Chem. Soc.* **129**, 8528 ('07)



- Electronic transitions from the current state to another occur stochastically based on the switching probability obtained by solving TDDFT equations

K -th excitation frequency

$$\Psi(\mathbf{r}, t) = \sum_J C_J^{(I)}(t) \Phi_J(\mathbf{r}; \mathbf{R}(t)) \quad C_I^{(I)}(0) = \delta_{I,J}$$

J -th adiabatic excited state

$$\frac{d}{dt} C_J^{(I)}(t) = - \sum_k C_k^{(I)}(t) \left(i\omega_K \delta_{JK} + \langle \Phi_J | \frac{\partial}{\partial t} | \Phi_K \rangle \right)$$

Electronic transition assisted by nuclei motion

QXMD Code

- **Quantum molecular dynamics (QMD) code developed by Prof. Fuyuki Shimojo at Kumamoto University in Japan**
- **Various eXtensions co-developed with USC-CACS: Nonadiabatic QMD, linear-scaling divide-&-conquer, parallelization, *etc.***
- **Unique features:**
 - > **Interatomic forces with electronic excitation to study photo-excited lattice dynamics**
Shimojo *et al.*, *Comput. Phys. Commun.* **184**, 1 ('13)
 - > **Range-separated hybrid exact-exchange functional for exciton binding**
Tawada *et al.*, *J. Chem. Phys.* **120**, 8425 ('04)
 - > **Lean divide-&-conquer density functional theory (LDF-DFT) with small $O(N)$ prefactor**
Shimojo *et al.*, *J. Chem. Phys.* **140**, 18A529 ('14)
 - > **Omni-directional multiscale shock technique (OD-MSST)**
Shimamura *et al.*, *Appl. Phys. Lett.* **107**, 231903 ('15); **108**, 071901 ('16)
- **Other features:**
 - > **Various functionals: spin-polarized, GGA+U, DFT+D, nonlocal correlation**
 - > **Nudged elastic band (NEB) method for energy-barrier calculation**
 - > **Berry-phase computation of polarization**

Software download site:

<https://magics.usc.edu/qxmd>

Current & Future Computing Platforms

- Won two DOE supercomputing awards to develop & deploy metascalable (“design once, scale on future platforms”) simulation algorithms (2017-2020)



- NAQMD & RMD simulations on full 800K cores

Innovative & Novel Computational Impact on Theory & Experiment

Title: “Petascale Simulations for Layered Materials Genome”

Principal Investigator:

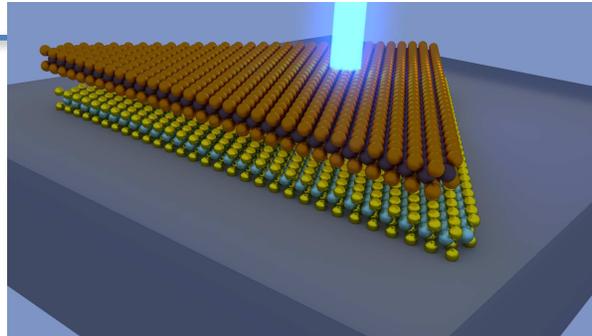
Aiichiro Nakano, University of Southern California

Co-Investigator:

Priya Vashishta, University of Southern California



786,432-core IBM Blue Gene/Q

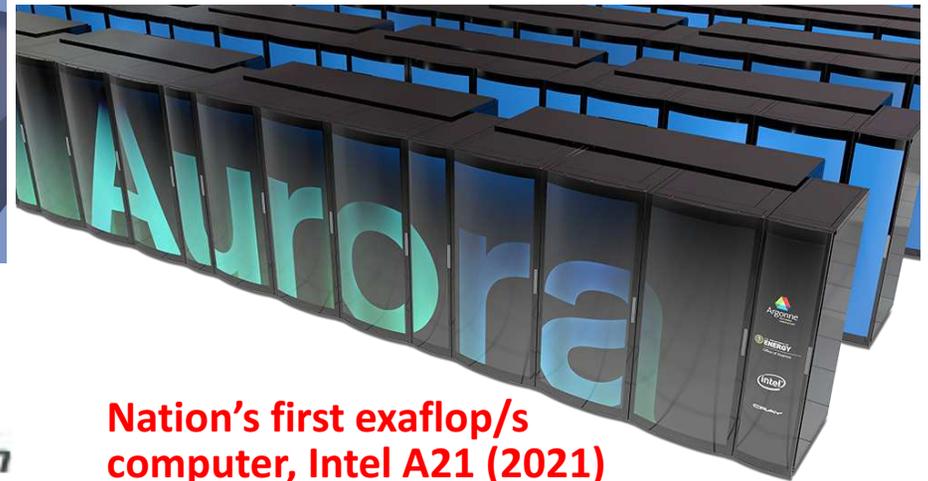


Early Science Projects for Aurora

Supercomputer Announced

Metascalable layered materials genome

Investigator: Aiichiro Nakano, University of Southern California



Nation's first exaflop/s computer, Intel A21 (2021)

exaflop/s = 10^{18} mathematical operations per second

- One of the 10 initial users of the next-generation DOE supercomputer

CACS@A21 in the Global Exascale Race



SUPERCOMPUTING

R. F. Service, *Science* 359, 617 ('18)

Design for U.S. exascale computer takes shape

Competition with China accelerates plans for next great leap in supercomputing power

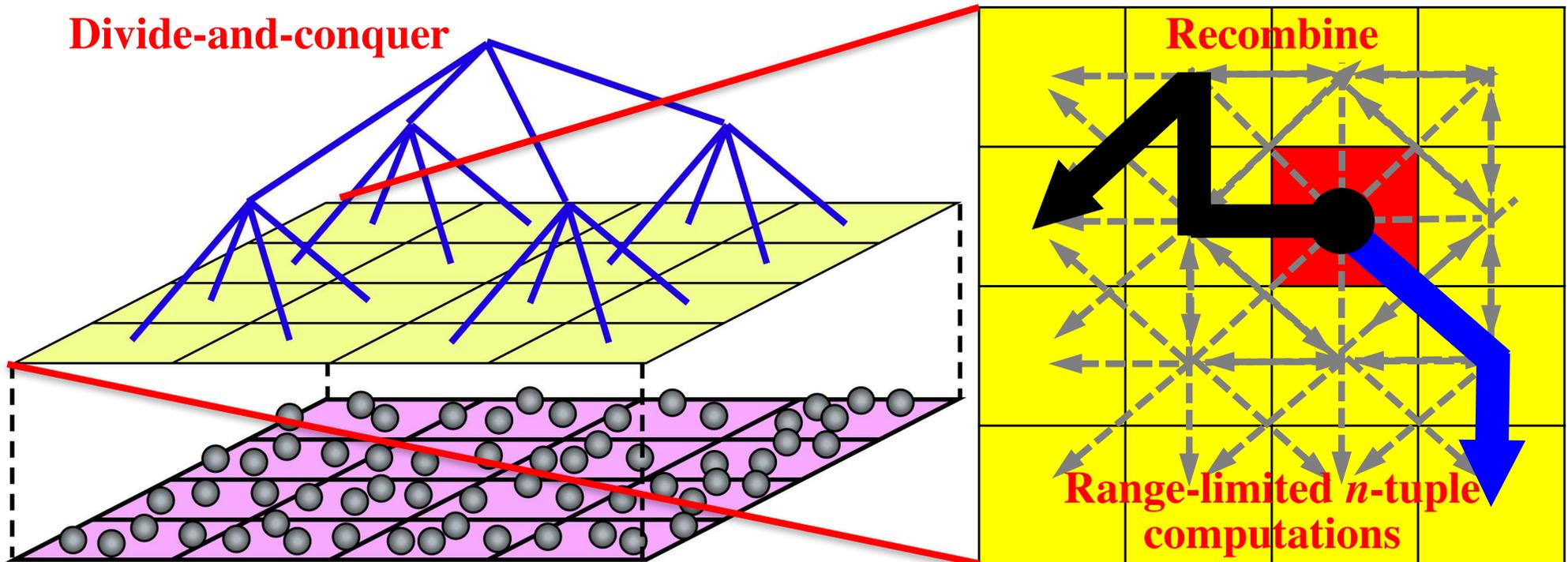
By **Robert F. Service**

In 1957, the launch of the Sputnik satellite vaulted the Soviet Union to the lead in the space race and galvanized the United States. U.S. supercomputer researchers are today facing their own

Lemont, Illinois. That's 2 years earlier than planned. "It's a pretty exciting time," says Aiichiro Nakano, a physicist at the University of Southern California in Los Angeles who uses supercomputers to model materials made by layering stacks of atomic sheets like graphene.

pace reflects a change of strategy by DOE officials last fall. Initially, the agency set up a "two lanes" approach to overcoming the challenges of an exascale machine, in particular a potentially ravenous appetite for electricity that could require the output of a small nuclear plant.

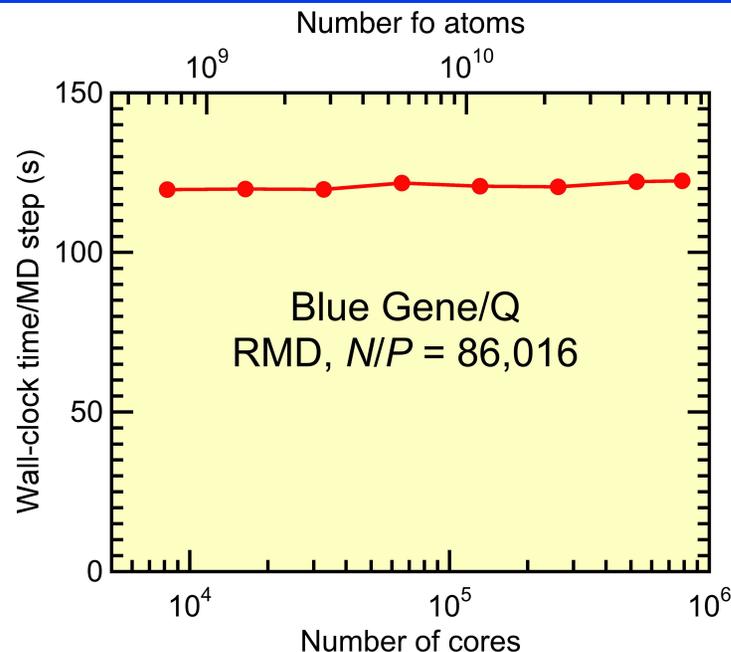
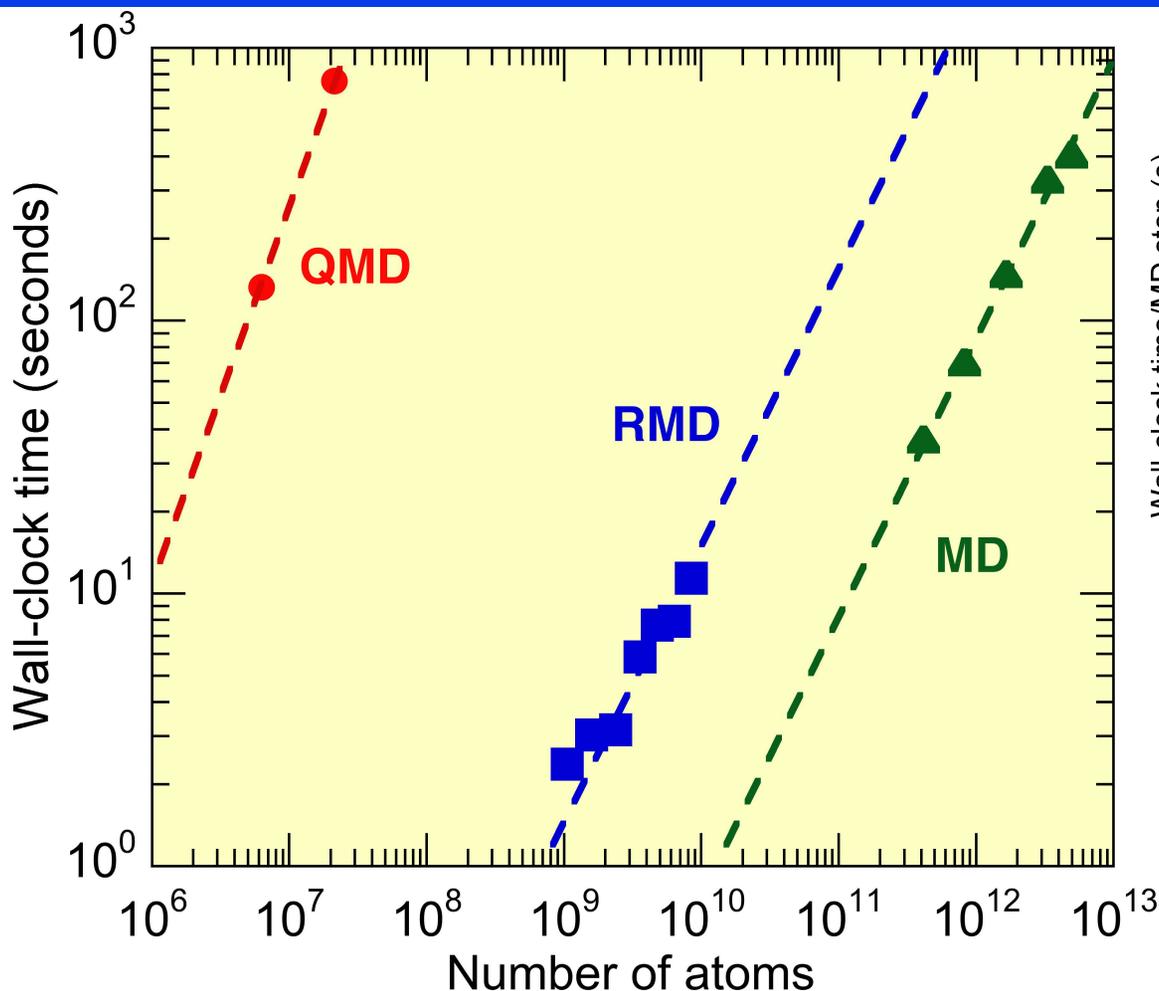
Divide-Conquer-Recombine (DCR) Engines



M. Kunaseth et al., ACM/IEEE SC13

- **Lean divide-&-conquer density functional theory (LDC-DFT) algorithm minimizes the prefactor of $O(N)$ computational cost**
F. Shimojo et al., *J. Chem. Phys.* **140**, 18A529 ('14); K. Nomura et al., *IEEE/ACM SC14*
- **Extended-Lagrangian reactive molecular dynamics (XRMD) algorithm eliminates the speed-limiting charge iteration**
K. Nomura et al., *Comput. Phys. Commun.* **192**, 91 ('15)

Scalable Simulation Algorithm Suite



QMD (quantum molecular dynamics): DC-DFT

RMD (reactive molecular dynamics): F-ReaxFF

MD (molecular dynamics): MRMD

- **4.9 trillion-atom space-time multiresolution MD (MRMD) of SiO_2**
- **67.6 billion-atom fast reactive force-field (F-ReaxFF) RMD of RDX**
- **39.8 trillion grid points (50.3 million-atom) DC-DFT QMD of SiC**
parallel efficiency 0.984 on 786,432 Blue Gene/Q cores

BES

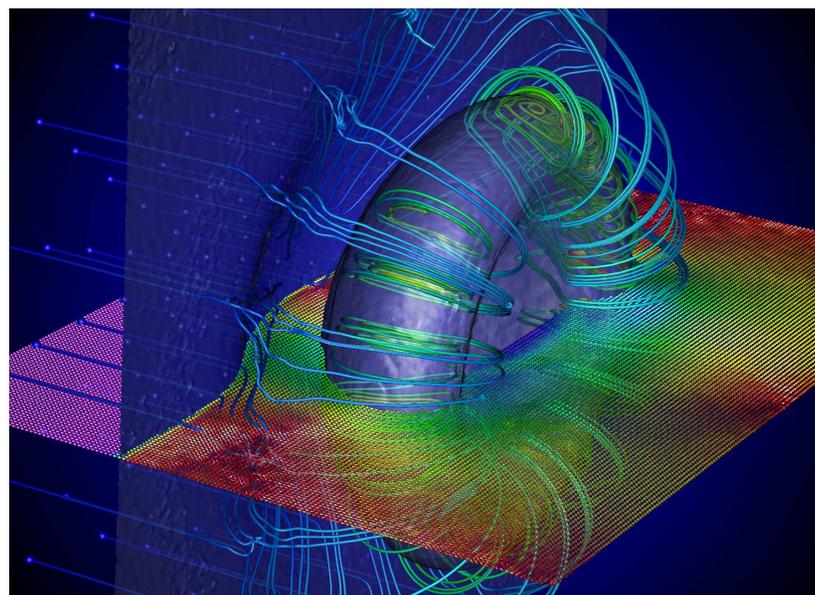
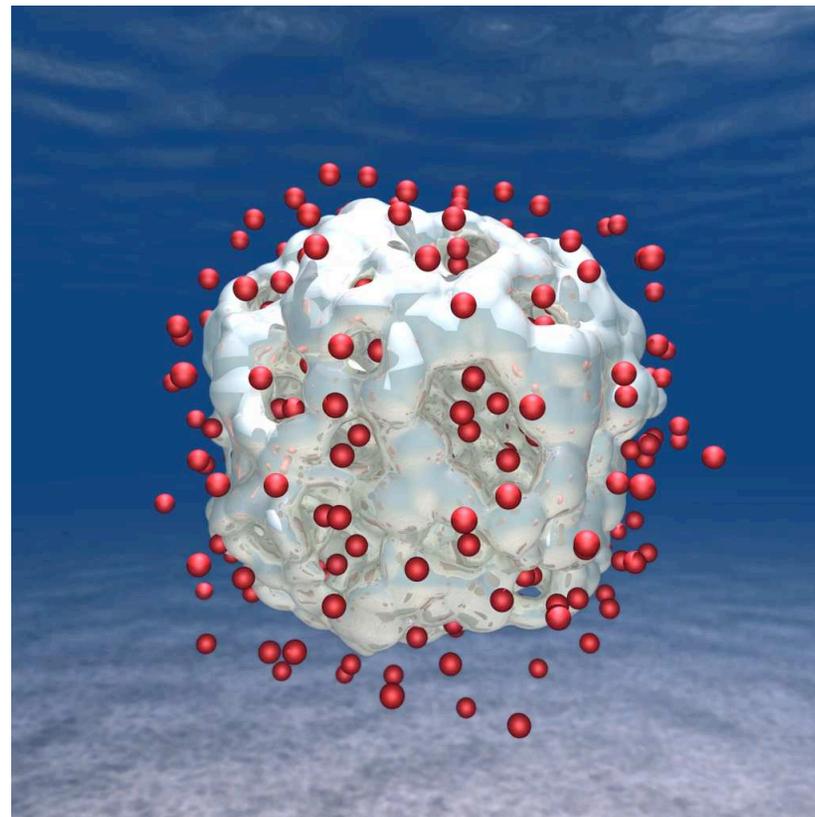
BASIC ENERGY SCIENCES

EXASCALE REQUIREMENTS REVIEW

An Office of Science review sponsored jointly by
Advanced Scientific Computing Research and Basic Energy Sciences

16,661-atom QMD
Shimamura *et al.*,
Nano Lett.
14, 4090 ('14)

10^9 -atom RMD
Shekhar *et al.*,
Phys. Rev. Lett.
111, 184503 ('13)

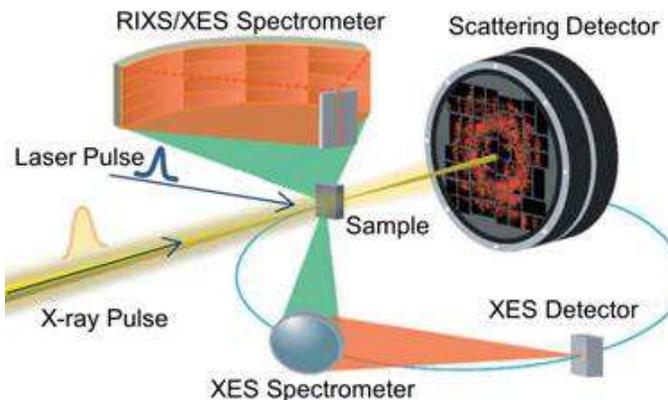
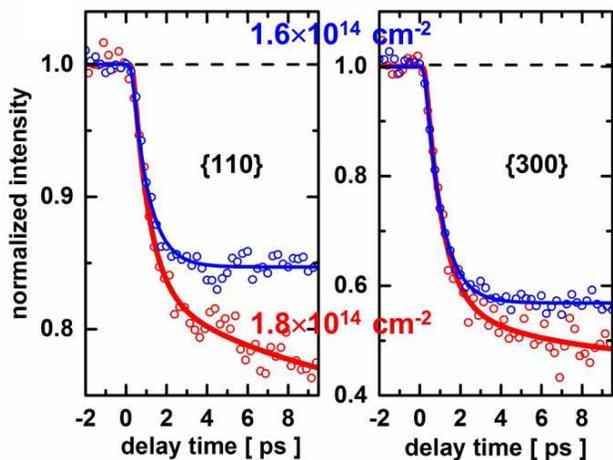


NOVEMBER 3-5, 2015

ROCKVILLE, MARYLAND



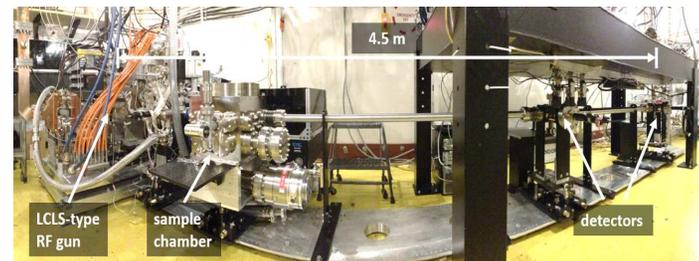
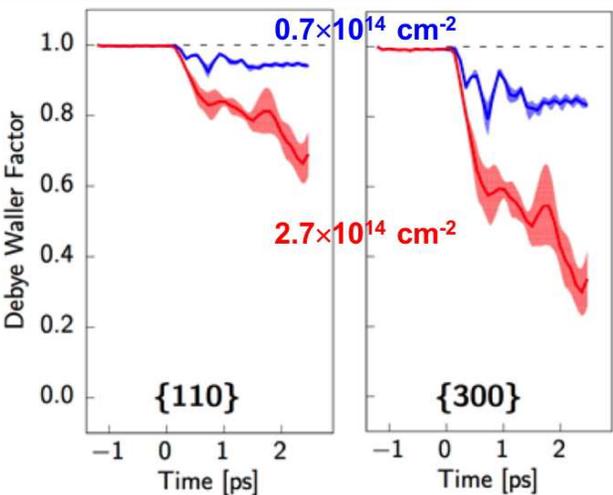
INCITE/AURORA-MAGICS-LCLS Synergy



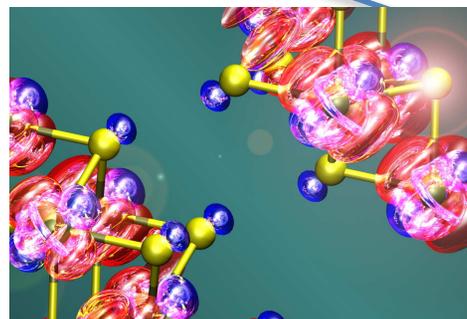
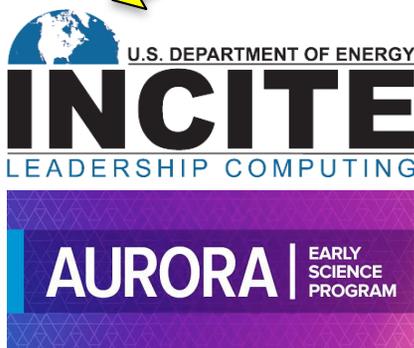
Linac Coherent Light Source

LCLS

DOE INCITE & Aurora ESP Awards

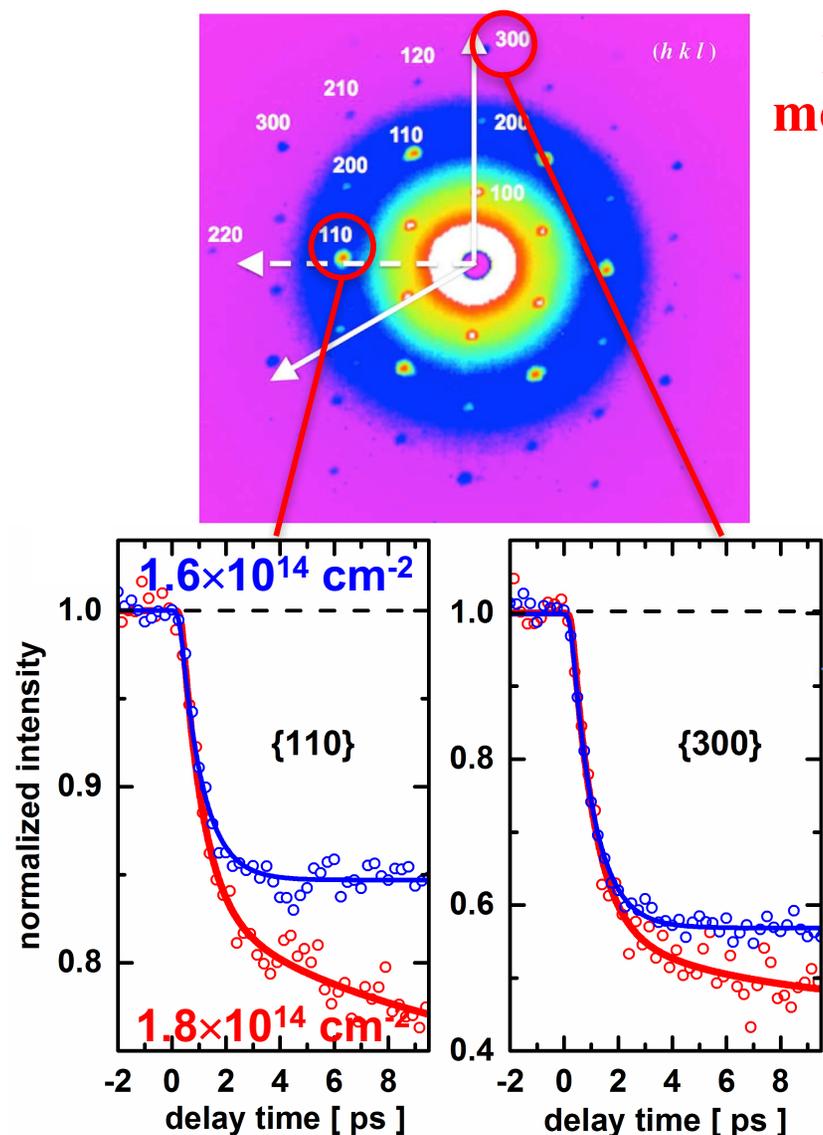


Ultrafast electron diffraction (UED) at SLAC

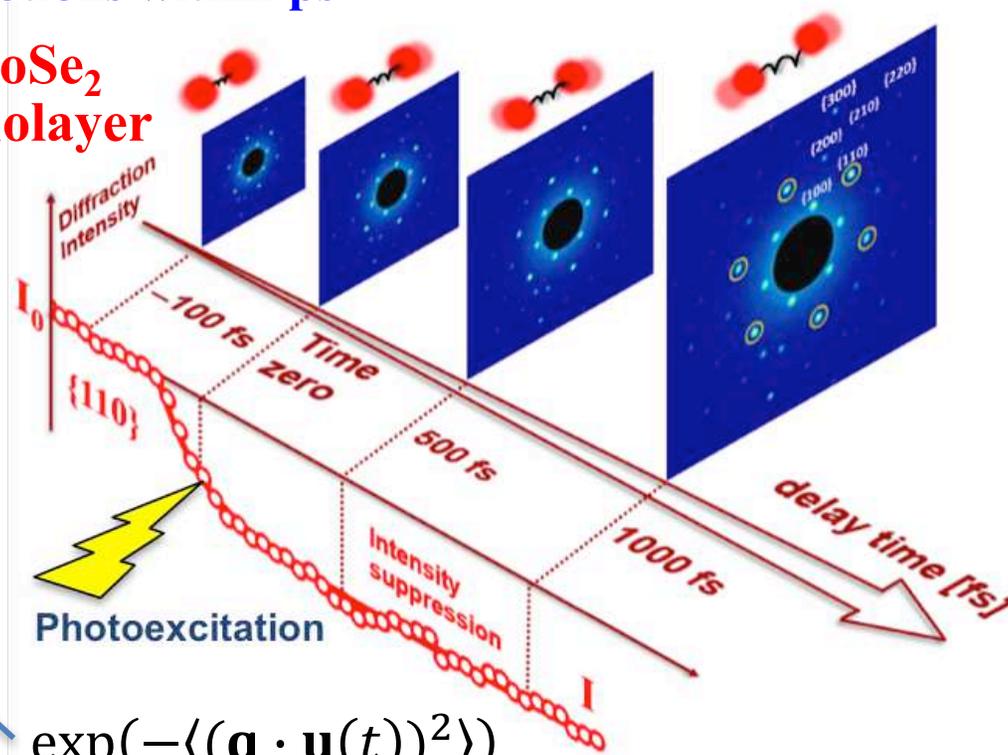


Ultrafast Coupled Electron-Lattice Dynamics

- Ultrafast electron diffraction experiment shows nearly perfect energy conversion from electronic excitation to lattice motions within ps



MoSe₂
monolayer



$$\exp(-\langle (\mathbf{q} \cdot \mathbf{u}(t))^2 \rangle)$$

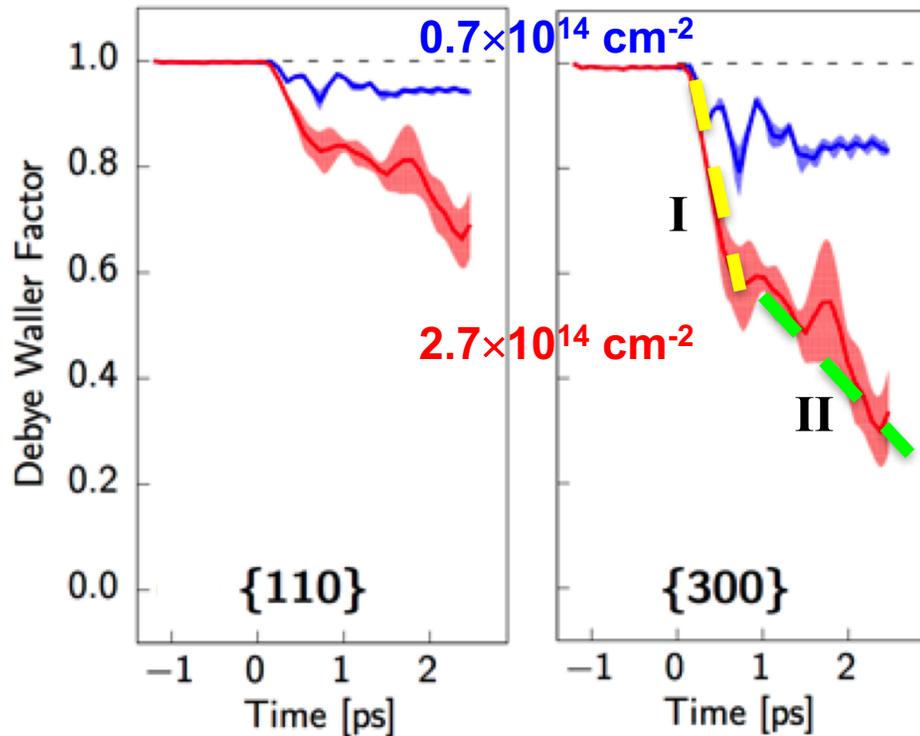
atomic displacement

- Dynamics of Debye-Waller factor reveals rapid disordering for both {300} & {110} peaks
- Transition from mono- to bi-exponential decay at higher electron-hole density

M.F. Lin *et al.*, *Nature Commun.* **8**, 1745 ('17)

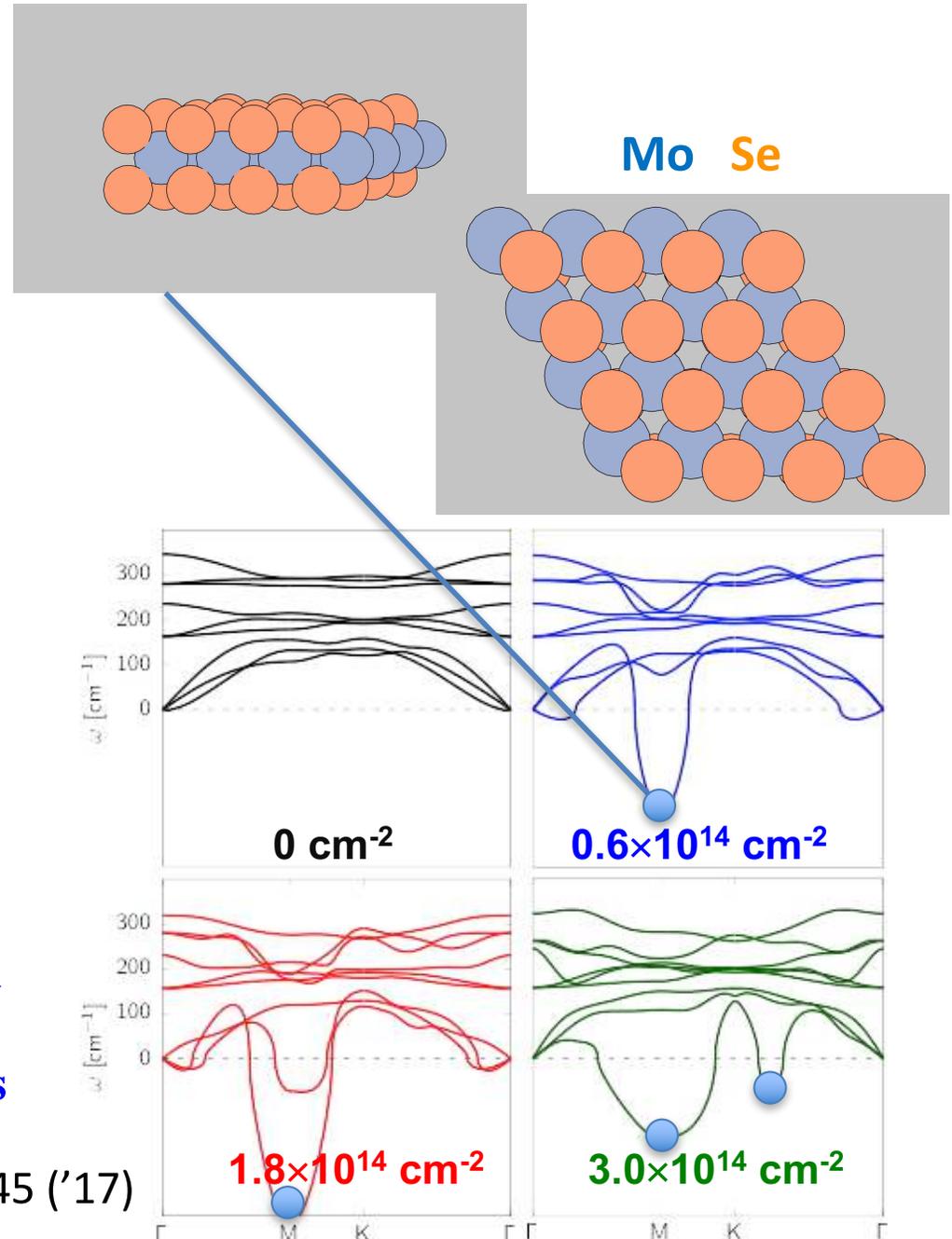
Strong Electron-Lattice Coupling

- NAQMD simulations reproduce (1) rapid photo-induced lattice dynamics & (2) mono- to bi-exponential transition at higher electron-hole density



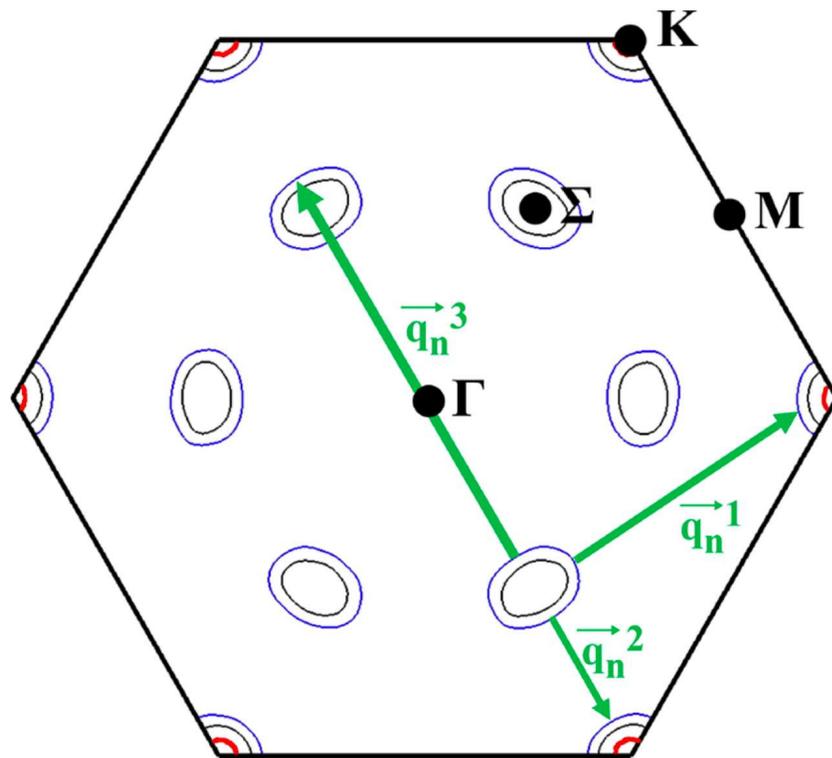
- Rapid lattice dynamics is explained by the softening of M-point ($1/2 \ 0 \ 0$) phonon
- Bi-exponential transition is explained by the softening of additional phonon modes at higher electron-hole densities

M.F. Lin *et al.*, *Nature Commun.* **8**, 1745 ('17)

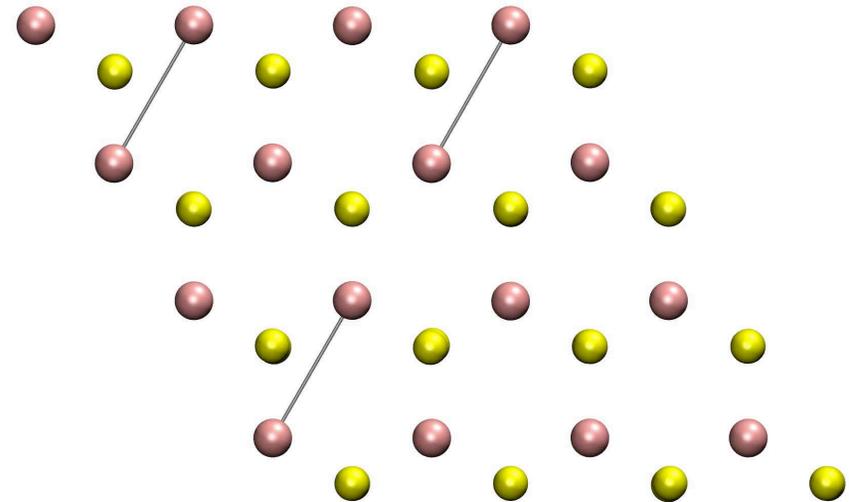
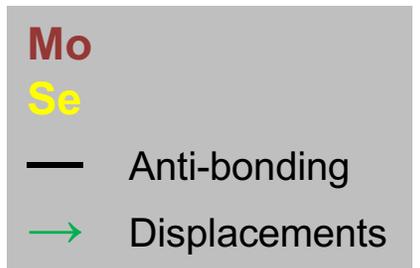


Electronic Origin of Phonon Softening

- Electronic Fermi surfaces at increased electron-hole densities $n(\text{e-h})$
- While the Fermi surface is localized at K-points at minimal excitation (**red**), it also occupies Σ -pockets at larger $n(\text{e-h})$ (**black & blue**), enabling electron scattering by emitting \vec{q}_n^1 (M), \vec{q}_n^2 (Σ) & \vec{q}_n^3 (K) phonons

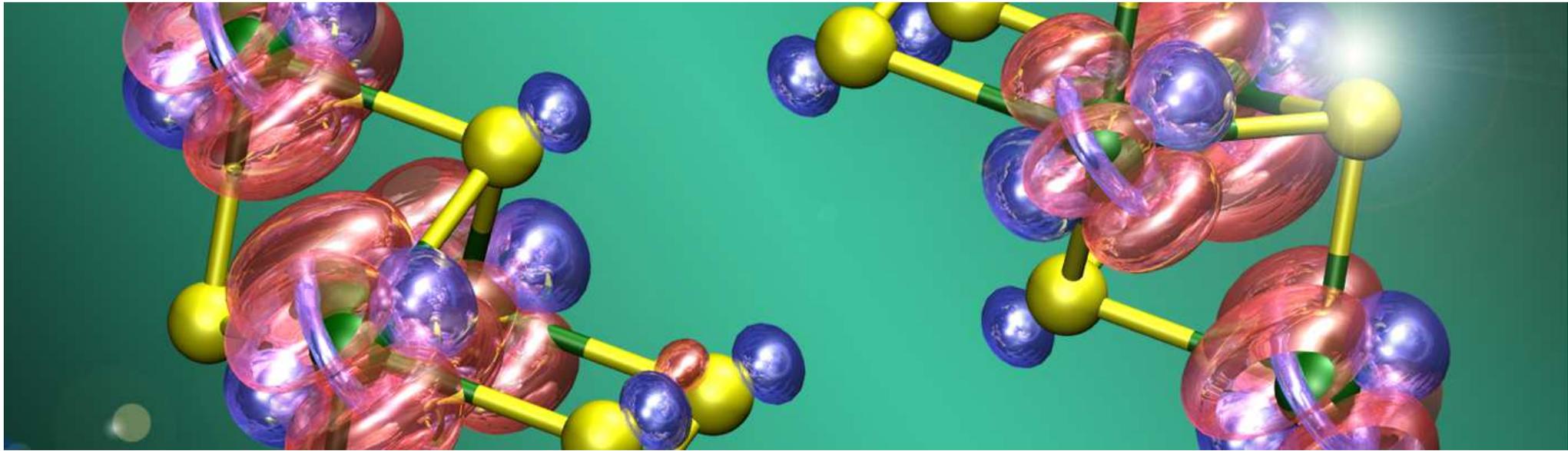


$$n(\text{e-h}) = 0.22, 1, 2 \times 10^{14} \text{ cm}^{-2}$$



- Increased anti-bonding upon photo-excitation drives the displacements of atoms

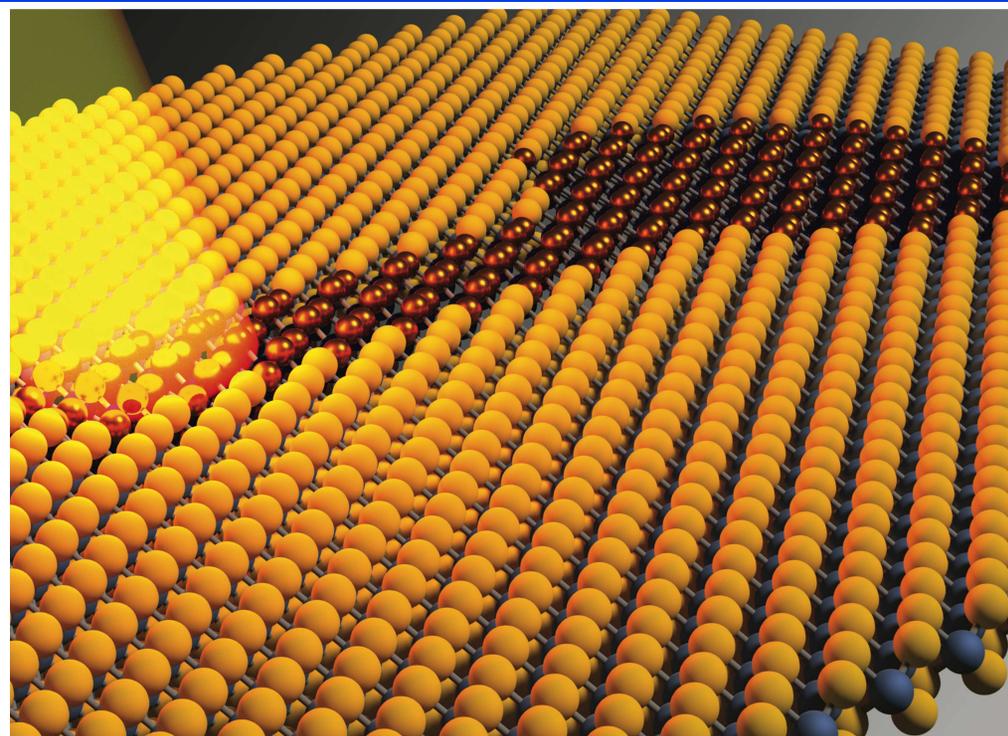
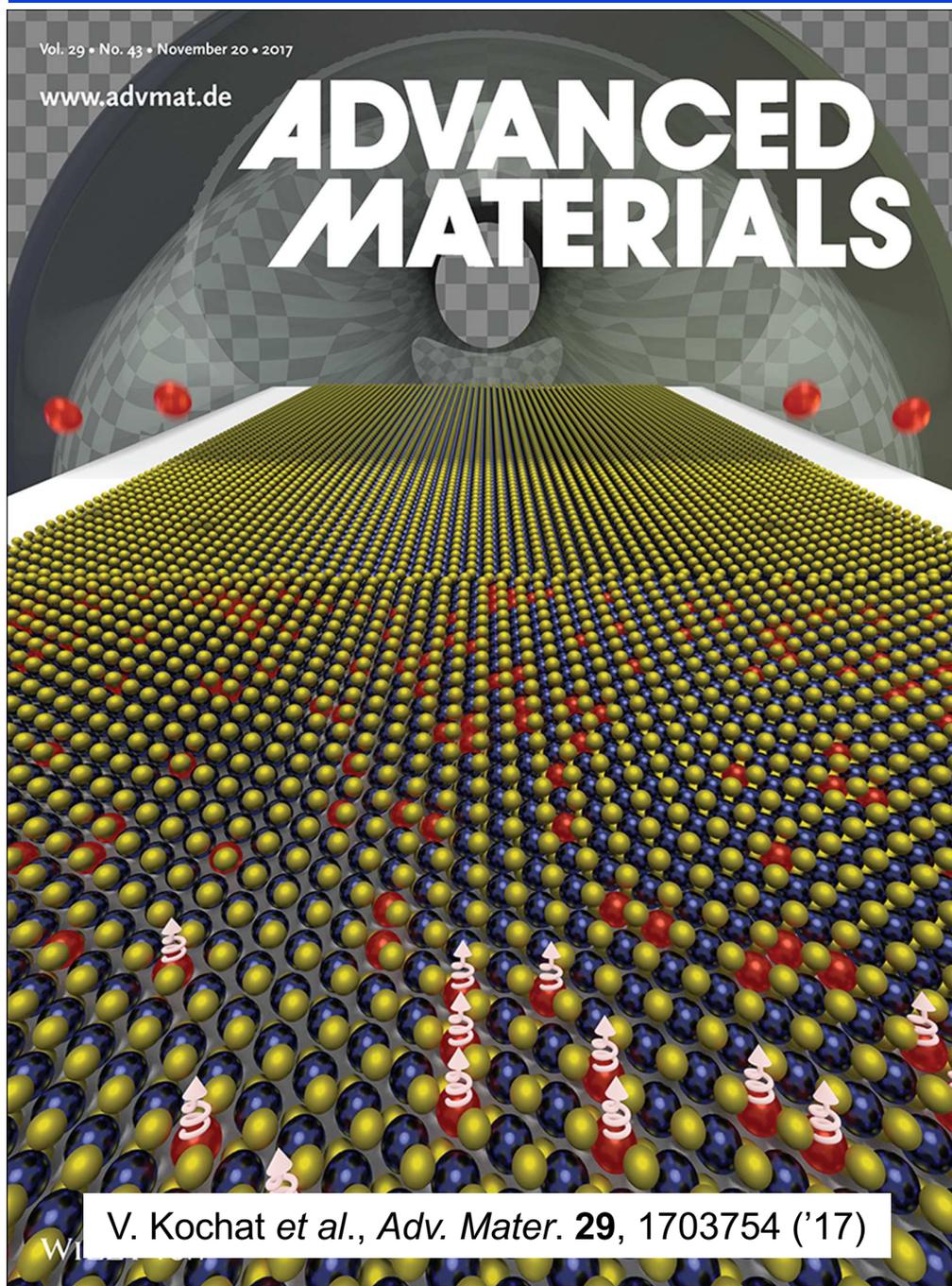
Simulation-Experiment Synergy



- **In the ultrafast ‘electron camera,’ laser light hitting a material is almost completely converted into nuclear vibrations — key to switching material properties on & off at will for future electronics applications**
- **High-end quantum simulations reproduce the ultrafast energy conversion at exactly the same space & time scales, & explain it as a consequence of photo-induced phonon softening**

Ming-Fu Lin, Vidya Kochat, **Aravind Krishnamoorthy**, **Lindsay Bassman**, Clemens Weninger, Qiang Zheng, Xiang Zhang, Amey Apte, Chandra Sekhar Tiwary, Xiaozhe Shen, Renkai Li, Rajiv Kalia, Pulickel Ajayan, Aiichiro Nakano, Priya Vashishta, Fuyuki Shimojo, Xijie Wang, David Fritz, Uwe Bergmann, *Nature Commun.* **8**, 1745 ('17)

MAGICS QMD Simulations

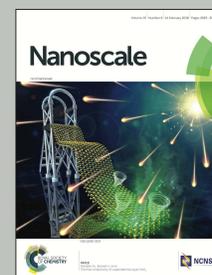


Showcasing research from Collaboratory for Advanced Computing and Simulations (CACS), University of Southern California, Los Angeles, USA.

Semiconductor–metal structural phase transformation in MoTe_2 monolayers by electronic excitation

Optical control of transformations between semiconducting and metallic phases of two-dimensional materials can open the door for phase patterning of heterostructures for 2D electronics and catalysis applications. This work shows how optically-induced changes to the electronic structure and Fermi surface of monolayer semiconductors couple to lattice distortions, resulting in a more facile phase transformation pathway. This work highlights photoexcitation as a viable technique for functionalizing these material systems.

As featured in:



See Aravind Krishnamoorthy et al., *Nanoscale*, 2018, 10, 2742.

A. Krishnamoorthy et al., *Nanoscale* 10, 2742 ('18)

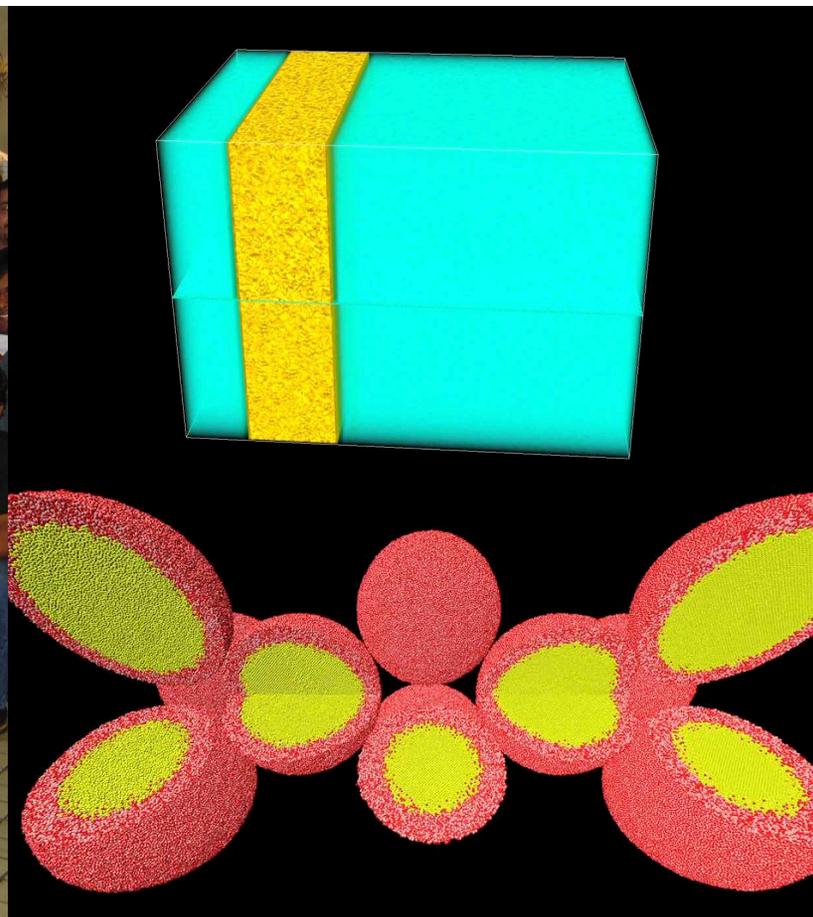


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Conclusion

1. Large spatiotemporal-scale quantum molecular dynamics simulations enabled by divide-conquer-recombine
2. Broad materials & energy applications



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